

Math 101, Littlefield
Homework: Arithmetic in Visual Notation and Single-Line Notation

Objective: practice and demonstrate mastery of two common notations for basic arithmetic.

Instructions: This homework provides an assortment of *arithmetic expressions*, written in ordinary *visual notation*. For each of these expressions, your tasks are to

1. Write one *equivalent expression* in *single-line notation*, using the minimum number of parentheses needed to specify the correct *order of operations* using the *PEMDAS* rules.
2. Write another *equivalent expression* in single-line notation, using parentheses around every *operator* and its *operands* to show the order of operations implied by PEMDAS.
3. *Evaluate* the expression. (That is, actually do the arithmetic and tell me what the *value* of the expression is. Because all three expressions are equivalent, they all must have the same value.)

Example:

First, let me use lots of words to spell out what I mean:

Suppose you have this expression in visual notation: $\frac{60 - 2 * 21}{2 + 1}$

In single line notation, with the minimum number of parentheses, it is:

$$(60-2*21)/(2+1)$$

Fully parenthesized to completely show the order of operations, it is:

$$((60-(2*21))/(2+1))$$

All of these expressions evaluate to the value 6.

Second, here is what I want you to actually write down and hand in, for me to check:

$$\frac{60 - 2 * 21}{2 + 1} = (60-2*21)/(2+1) = ((60-(2*21))/(2+1)) = 6$$

Problems:

1.
$$\frac{50 - 4 * 2}{6 + 1}$$

2.
$$\frac{45}{3 * 5}$$

3.
$$\frac{1}{2} \cdot 49 \cdot (11 + 13)$$

4.
$$\frac{1}{3} \cdot 10 \cdot 20 \cdot 30$$

5.
$$\frac{2 \cdot (10 + 5)}{7 + 8}$$

6.
$$100 / 5 / 2 * 4$$

7.
$$\frac{4 \cdot 21 + 7}{14 - 7}$$

8.
$$\frac{4 \cdot 21 + 7 \cdot 13 + 7}{13}$$

9.
$$\frac{-2 \cdot 4 + 4}{4}$$

10.
$$\frac{1}{\frac{1}{3} + \frac{1}{6}}$$