

# Examples of Variety in Math Notation

From <http://en.wikipedia.org/wiki/Volume>:

Shape	Equation	Variables
A <a href="#">cube</a>	$a^3$	$a$ = length of any side (or edge)
A rectangular prism:	$l \cdot w \cdot h$	$l$ = length, $w$ = width, $h$ = height
A <a href="#">cylinder</a> :	$\pi r^2 h$	$r$ = radius of circular face, $h$ = height
A general <a href="#">prism</a> :	$B \cdot h$	$B$ = area of the base, $h$ = height
A <a href="#">sphere</a> :	$\frac{4}{3}\pi r^3$	$r$ = radius of sphere which is the <a href="#">integral</a> of the <a href="#">Surface Area</a> of a <a href="#">sphere</a>
An <a href="#">ellipsoid</a> :	$\frac{4}{3}\pi abc$	$a$ , $b$ , $c$ = semi-axes of ellipsoid
A <a href="#">pyramid</a> :	$\frac{1}{3}Bh$	$B$ = area of the base, $h$ = height of pyramid
A <a href="#">cone</a> (circular-based pyramid):	$\frac{1}{3}\pi r^2 h$	$r$ = radius of <a href="#">circle</a> at base, $h$ = distance from base to tip
Any figure ( <a href="#">calculus</a> required)	$\int A(h) dh$	$h$ = any dimension of the figure, $A(h)$ = area of the cross-sections perpendicular to $h$ described as a function of the position along $h$ . This will work for any figure if its cross-sectional area can be determined from $h$ (no matter if the prism is slanted or the cross-sections change shape).

Notice the inconsistent use of centered dot versus implied multiplication, even on this one page. You're expected to figure out that  $bc$  means  $b$  times  $c$  in the sixth equation, but the apparently similar  $dh$  in the last equation is really a completely different symbolism that means "delta  $h$ ". You're also expected to figure out that  $A(h)$  in that last equation does not mean a value  $A$  times some value  $h$ , but rather that  $A$  is a function that turns some value  $h$  into a completely different value " $A$  of  $h$ ", whose meaning in this case is that  $h$  is a position and  $A(h)$  is a cross-sectional area at that position. The  $A(h)$  functional notation is sometimes used in ordinary algebra also, but it really becomes important in higher math such as trig and calculus. Nonetheless, there's a common concept: both  $h$  and  $A(h)$  represent ordinary numbers, we just don't happen to know their values yet.

As a further example, consider <http://en.wikipedia.org/wiki/Fahrenheit> :

	from Fahrenheit	to Fahrenheit
<a href="#">Celsius</a>	$[^{\circ}\text{C}] = ([^{\circ}\text{F}] - 32) \times \frac{5}{9}$	$[^{\circ}\text{F}] = [^{\circ}\text{C}] \times \frac{9}{5} + 32$

Here, the notation " $[^{\circ}\text{C}]$ " denotes a single variable whose meaning is "temperature in degrees Celsius". So, the notation  $[^{\circ}\text{C}] = ([^{\circ}\text{F}] - 32) \times \frac{5}{9}$  in this context means exactly same thing as the notation  $C = (F-32)*5/9$  that we encountered earlier in class.

Not to harp on the point, but...

**There is no such thing as The Language of Mathematics. There are a bunch of dialects. Be sure you know what those symbols mean, at the place they're being used!**